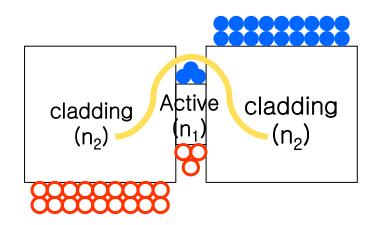
Two conditions for lasing: (1)
$$\Gamma g_{th} = \alpha_m + \alpha_{int}$$
 and (2) $\frac{\lambda}{n_{eff}} = \frac{2L}{m}$

There can be several lasing modes: several λ 's satisfying above conditions.

(1) Multi-mode waveguide

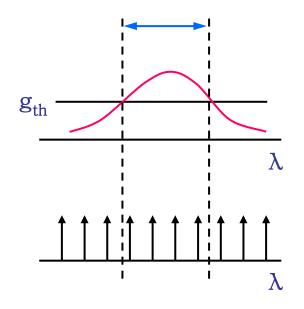


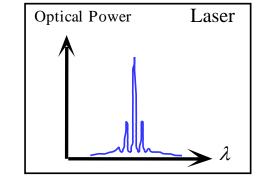
Different modes have different n_{eff}.

=> Design for single guided mode.

TE, TM modes?

Several cavity modes





Mode separation

From
$$e^{-j2nk_0L} = 1 \Rightarrow 2n_{\text{eff}}k_0L = 2m\pi$$

$$\Delta(n_{\rm eff}k_0)L = \pi \implies \Delta(n_{\rm eff}k_0) = \frac{\pi}{L}$$

$$\lambda = n_{eff} \frac{2\pi}{k_0} \therefore \Delta \lambda = \frac{\delta \lambda}{\delta k_0} \Delta k = -n_{eff} \frac{2\pi}{k_0^2} \Delta k = -\frac{\lambda^2}{2n_{eff} L}$$

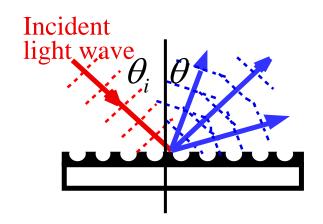
$$\frac{\lambda}{n_{\text{eff}}} = \frac{2L}{m} \text{ for } g(\lambda) > g_{\text{th}}$$

With typical semiconductor lasers with cleaved facets, $\Delta\lambda$ is less than gain bandwidth => multi lasing modes

→ Fabry-Perot laser

Single-mode laser for long-distance, high-speed optical communications?

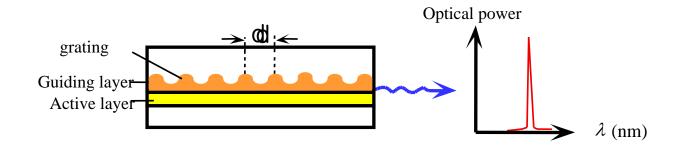
Use another type of mirror: Grating



$$d(\sin \theta - \sin \theta_i) = m \cdot \lambda$$
For $\theta_i = 90^\circ$ and $\theta = -90^\circ$,
$$d = m\frac{\lambda}{2}$$

How to implement diffraction grating within semiconductor laser?

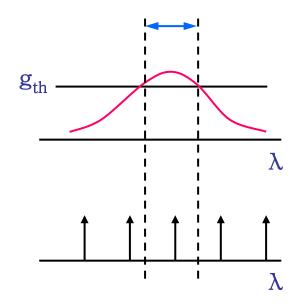
Distributed Feedback (DFB) Laser



$$d = m \frac{\lambda}{2n_{\text{eff}}}$$
 (typically m=1)

Another approach:

Make L very small so that $\Delta\lambda$ larger than gain bandwidth



$$\left|\Delta\lambda\right| = \frac{\lambda^2}{2n_{eff}L}$$

gain bandwidth: in the order of 10nm

 λ : 1.5 μ m

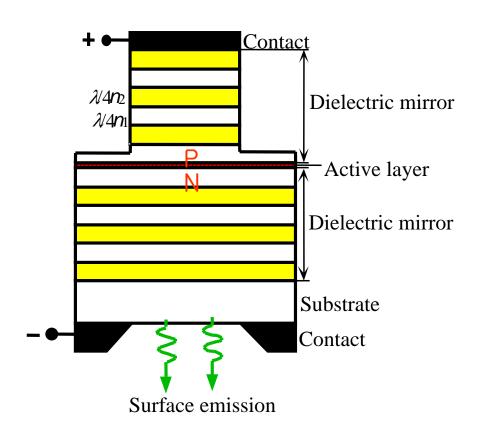
 $n_{eff}: 3.5$

 $L \sim 30 \mu m$;

Not easy to fabricate by cleaving

From
$$\alpha_{\rm m} = \frac{1}{L} \ln \frac{1}{R}$$
, too much mirror loss

Solution: Very short cavity vertical lasers with very high reflectivity mirrors (VCSEL: Vertical Cavity Surface Emitting Laser)



In semiconductor fabrication, vertical thickness can be very precisely controlled.

Dielectric mirror can have high reflectivity approaching R=1.

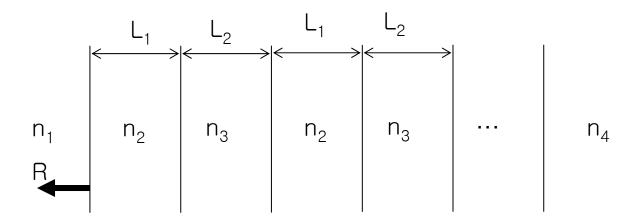
From
$$\alpha_{\rm m} = \frac{1}{L} \ln \frac{1}{R}$$
,

 $\alpha_{\rm m}$ can be made small if R approaches 1.

VCSELs are cheap because it is easy to make.

Review: High-Reflection Coating => Dielectric mirror

Repeat the quarter-wavelength pair m times.



$$R = \left(\frac{n_1 - \left(\frac{n_2}{n_3}\right)^{2m} n_4}{n_1 + \left(\frac{n_2}{n_3}\right)^{2m} n_4}\right)^2 \qquad \text{If } n_2 > n_3, \ R \sim \left(\frac{-\left(n_2/n_3\right)^{2m} n_4}{+\left(n_2/n_3\right)^{2m} n_4}\right)^2 = 1$$

$$\text{If } n_2 < n_3, R \sim \left(\frac{n_1}{n_1}\right)^2 = 1$$

Exercise Problems:

Prob. 9, Prob. 12, Prob. 15, Prob. 18, Prob. 20, Prob. 23 in Part 3

Schedule for coming weeks:

- Nov. 21: Quiz 8, Lect. 22
- Nov. 23: Lect. 23
- Nov. 28: Quiz 9, Research Presentation (고민수, 윤순준)
- Nov. 30: Research Presentation (이명재, 홍문기)
- Dec. 5: Research Presentation (오택일)
- →25 minutes for each presentation

Special Topic Presentation

40 min. presentation on one of following topics:

- Nonlinear Optics in Fiber (이명재)
- Silicon Raman Laser (홍문기)
- Photonic Crystal (윤순준)
- Slow Light (고민수)
- -Quantum Cascade Lasers (오택일)

-Dec. 5: 고민수

- Dec. 7: 윤순준

- Dec. 12: 이명재, 홍문기

- Dec. 14: 오택일

→ Dinner together on Dec. 14